



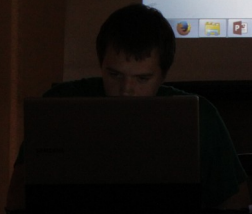
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## THE QUALITY INSPECTION METHOD OF SECURITY HOLOGRAMS

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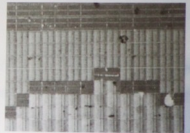


## Objective

The subject of the work is developing of method, based on objective assessment about the quality of security holograms

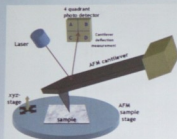
The main parameters of the elementary grating:

- spatial frequency  $\nu_x$ ;
- grating depth  $d$ ;
- number of periods in the grating  $N$ ;
- grating orientation  $\varphi$ .

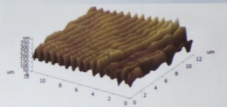


## Methods of security hologram quality inspection

1) Method based on directly measurements of the diffraction grating parameters with atomic force microscope.



Disadvantages: time-consuming processing of results, expensive equipment.



2) Method based on indirectly measurements of the diffraction grating parameters.

### Known relationships:

- For a given value of wavelength  $\lambda$  and incidence angle  $\alpha$  the intensity distribution  $I$  over the diffraction orders of the phase grating depends on the grating depth  $d$ ;
- For a given value of wavelength  $\lambda$  and incidence angle  $\alpha$  the value of diffraction orders angles  $\beta_{\pm 1}$  depends on the value of the spatial frequency  $\nu_x$ ;
- The orientation of the plane in which diffraction orders are located depends on the angle orientation diffraction grating  $\varphi$ ;
- Angular size  $\Delta\beta_{\pm 1}$  of the diffraction orders depends on the number of periods in the grating  $N$ .

### Assumptions of the mathematical model description:

- elementary phase diffractive gratings are sinusoidal;
- effects caused by secondary re-reflections are negligible;
- the scalar diffraction theory is used.

The equation of the phase grating surface

$$z = A \cdot \left(1 - \cos \frac{2\pi x}{T}\right) = 2A \sin^2 \frac{\pi x}{T}$$



Wave amplitude distribution

$$U = U_0 \cdot U_1 \cdot U_2$$

$$U_1 = \int_0^T e^{ik_1 x} dx$$

$$U_2 = \sum_{n=0}^N e^{ik_2 n x}$$

$$\Delta_0 = T(\sin \alpha + \sin \beta)$$

Intensity distribution

$$I = I_0 \cdot I_1 \cdot I_2$$

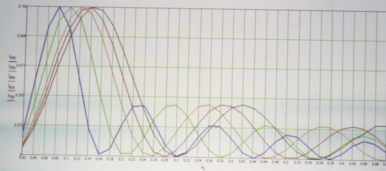
$$I_1 = |U_1|^2 = \frac{\sin^2 \left( \pi \frac{N \Delta_1}{\lambda} \right)}{\sin^2 \left( \frac{\pi \Delta_1}{\lambda} \right)}$$

$$I_2 = |U_2|^2 = \frac{\sin^2 \left( \frac{\pi \Delta_2}{\lambda} \right)}{\sin^2 \left( \frac{\pi \Delta_2}{\lambda} \right)}$$

The results of mathematical modeling

Graphs of the ratio between intensity distribution  $I$  in the first order of diffraction and the grating depth  $d$  for normal incidence of radiation

$$\alpha=0, T_x = 1,5 \mu m, \lambda = 400, 500, 600, 650, 700 \text{ nm}$$

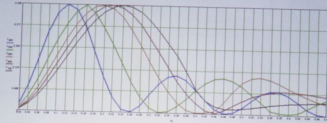




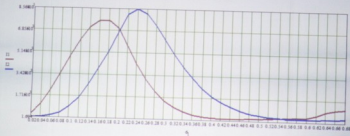
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$\alpha = 0$ ,  
 $\lambda = 400, 500, 600,$   
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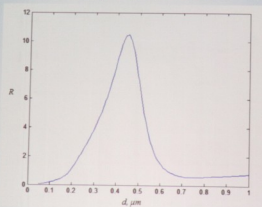


$\alpha = 60^\circ$ ,  
 $\lambda = 405 \text{ nm}$



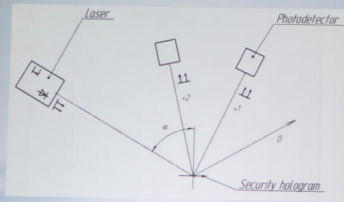
To improve the accuracy of the method, we use the relationship  $R$  between intensity distributions of the 1st and 2nd diffraction orders

Graph of the ratio between  $R$  and the grating depth  $d$   
for  $T_x = 1 \mu\text{m}$ ,  $\lambda = 405 \text{ nm}$





Functional scheme showing principal of the method



## Conclusions

- 1) The possibility of security holograms quality inspection based on the proposed method of indirect measurement of grating parameters is confirmed.
- 2) Relations for defining the parameters of the grating are derived.