



清华大学  
Tsinghua University



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## Fully computed holographic stereogram

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**HOLOLAB**

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# Holographic 3D display

- ❑ Reconstruction of whole optical wavefront



- ❑ Can provide all the depth cues



binocular cues



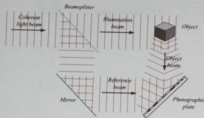
motion parallax  
& occlusion



accommodation

## Computer-generated holograms

- Without using interference of coherent light



- Can display both real and virtual scenes



Mathematical representation

Algorithm



Hologram

## Can CGHs be more photorealistic?



By Henrik Wann Jensen

Mathematical representation

Render

Image

Lighting

Geometry

Texture

Shadow

Reflection



Wavefront

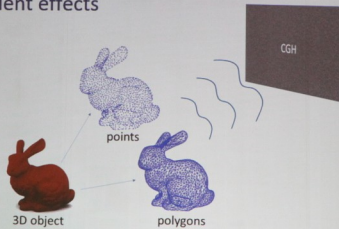
Computer graphics

+

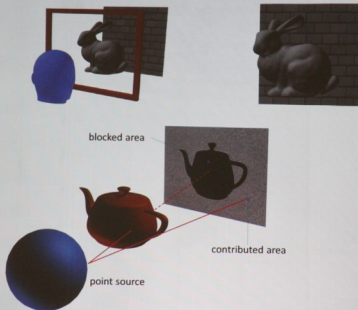
CGH algorithm

## Physically based algorithms

- Modeling optical wave transmission
- Discretizations of 3D scene (points and facets)
- Difficult to express occlusion and other view dependent effects



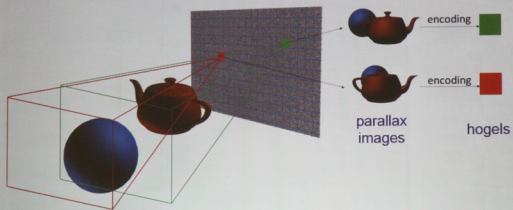
## Motion parallax and occlusion effect



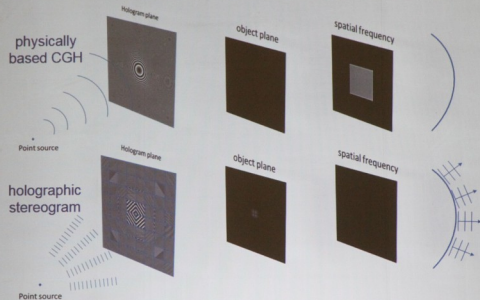


## Holographic stereogram

- Computer graphics implemented
- Lack of depth information



## Phase profiles of CGHs



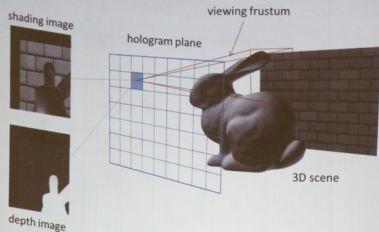


## Fully-computed holographic stereogram

Physically based  
algorithm

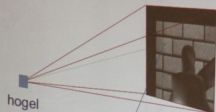
+

Holographic stereogram  
based algorithm



Hao Zhang, et al. "Fully computed holographic stereogram based algorithm for computer-generated holograms with accurate depth cues," *Opt. Express* 23, 3901-3913 (2015)

## Geometrical transmission

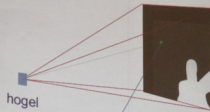


$A$  amplitude

$$\sin \theta_{\max} = f_{\max} \lambda = \frac{1}{2d} \lambda$$

$$h_{\text{hogel}}(x, y) = \sum_{j=1}^N \frac{A_j}{r_j} \exp[i(kr_j + \phi_j)]$$

$$r_j = \sqrt{(x-x_j)^2 + (y-y_j)^2 + z_j^2}$$



$(\theta_x, \theta_y, z_p)$

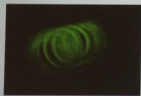
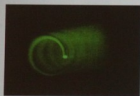
$$z_o = z_p$$

$$x_o = z_o \tan \theta_x$$

$$y_o = z_o \tan \theta_y$$

$(x_o, y_o, z_o)$  coordinates

## Reconstructions using LCOS

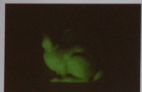


## High-resolution CGH

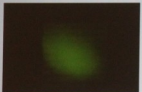


Parameter	Value
Number of pixels	$4 \times 10^8$ (20,000 × 20,000)
Pixel pitch	1 micron
Hologram size	20mm×20mm
Modulation type	Binary amplitude
Wavelength	532nm
Viewing angle	30.9°

# Optical reconstructions



Focusing on the bunny



Focusing on the wall



Left

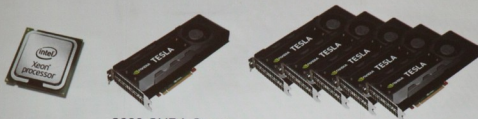


Center



Right

## Acceleration

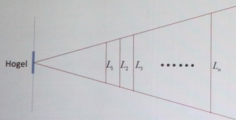
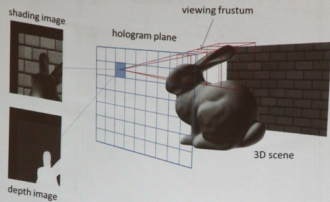


2688 CUDA Cores

CGH <sub>(1024x1024)</sub>	CPU	GPU	5GPU
1000 points	83.9s	60ms	13ms
5000 points	427.9s	298ms	65ms
10000 points	847.4s	605ms	129ms
50000 points	4203.4s	3002ms	664ms

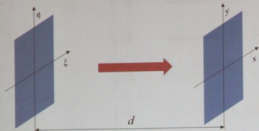


## Layered holographic stereogram



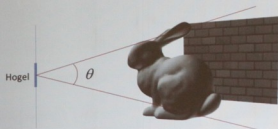
$$H = \sum_{i=1}^n \text{Fresnel}^{-1}(L_i)$$

## Sampling in Fresnel propagation



$$\Delta x = \frac{\lambda d}{N \Delta \xi}$$

$$x \in \left[ -\frac{\lambda d}{2 \Delta \xi}, \frac{\lambda d}{2 \Delta \xi} \right]$$



$$\tan \frac{\theta}{2} = \frac{\lambda}{2 \Delta \xi}$$

## Reconstructions

Point based



Layer based



Calculation time: 3390s VS 21s (CPU)  
2.42s VS ? (GPU)

## Conclusion

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- Computer graphics rendering can be used in CGH calculation to improve the image fidelity
- More depth information can be reconstructed by integrating physically based algorithm and holographic stereogram
- Use GPU for acceleration

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Thank you